



# Reproducibility Study: Equal Improvability

## A New Fairness Notion Considering the Long-Term Impact

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# Motivation

- Most of existing fairness notions only consider immediate fairness, without taking into account the equal improvement possibility of the members of the different groups.
- In contrast, Equal Improvability (EI) is an effort-based fairness notion that concerns itself with long-term fairness.
- Real world applications could be found in areas where the group members can improve their features and be re-labelled, e.g. loan approval, college admissions.

# Equal Improvability

Group 0's rejected samples are much closer to the boundary than Group 1 (less effort to cross the boundary)



Disparity in Improvability  
(unfairness)

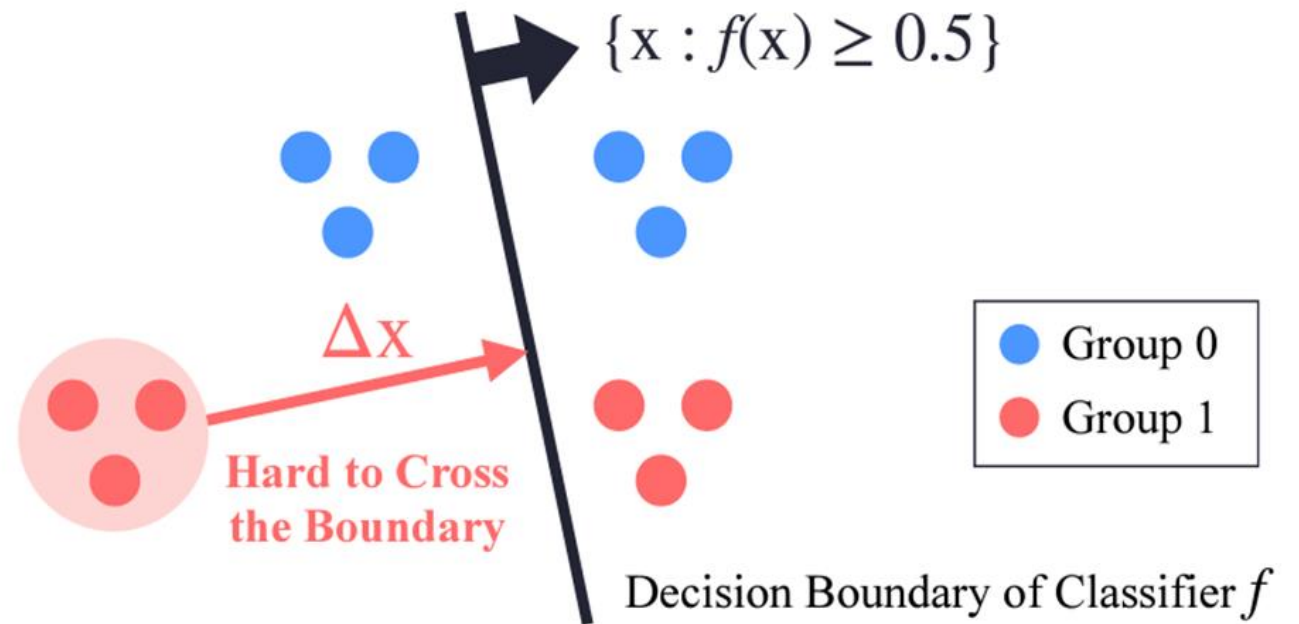
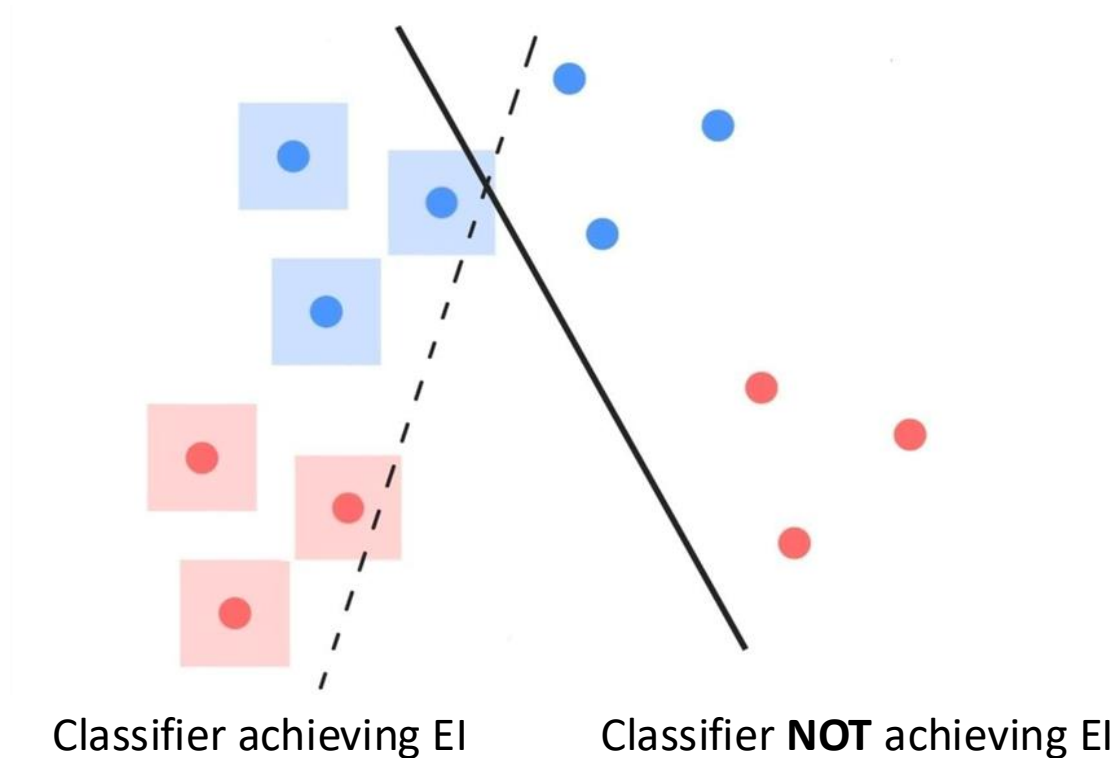


Image Source: Guldogan et al, 2023

# Equal Improvability

Effort-based fairness notion that aims to balance the potential acceptance rates for rejected applicants across various groups, given a fixed amount of effort.



# Equal Improvability Penalty

$$\min_{f \in \mathcal{F}} \left\{ (1 - \lambda) \frac{1}{N} \sum_{i=1}^N \ell(y_i, f(x_i)) + \boxed{\lambda U_\delta} \right\}$$

• Covariance-based penalty:  $(\text{Cov}(z, \max_{\|\Delta \mathbf{x}_I\| < \delta} f(\mathbf{x} + \Delta \mathbf{x}) \mid f(\mathbf{x}) < 0.5))^2$

• KDE-based penalty:  $|KDE(EI \text{ Disparity})|$

• Loss-based penalty:  $\sum_{z \in \mathcal{Z}} \left| \frac{1}{|I_{-,z}|} \sum_{i \in I_{-,z}} \ell(1, \max_{\|\Delta \mathbf{x}_I\| \leq \delta} f(\mathbf{x}_i + \Delta \mathbf{x}_i)) \right| - \sum_{z \in \mathcal{Z}} \frac{I_{-,z}}{I_-} \tilde{L}_z \Big|$

# Claims of the original paper

**Claim 1:** A classifier obtained by each of the three proposed EI ensuring methods, has a significantly smaller EI disparity value than the ERM (Empirical Risk Minimization) approach and a comparable error.

**Claim 2:** Most existing methods have an adverse effect on long-term fairness, while EI continues to enhance it.

**Claim 3:** The introduced methods of achieving Equal Improvability prevent an over-parametrized classifier from overfitting the data.

# Experimental setup - Datasets

| Datasets                          | Samples | Classes | Sensitive attrs. |
|-----------------------------------|---------|---------|------------------|
| Synthetic                         | 20,000  | 2       | 1                |
| German Statlog Credit             | 1,000   | 2       | 1 & 2            |
| ACS-Income-CA                     | 195,665 | 2       | 1 & 2            |
| Default of Credit<br>Card Clients | 30,000  | 2       | 1                |

New dataset!

# Experimental setup - Models

- Logistic Regression
- Multilayer Perceptron Model



# Reproducibility experiments

1

El Disparity and Loss  
value check

(Claim 1)

2

Long-term  
(un)fairness check

(Claim 2)

3

Overfitting  
robustness check

(Claim 3)

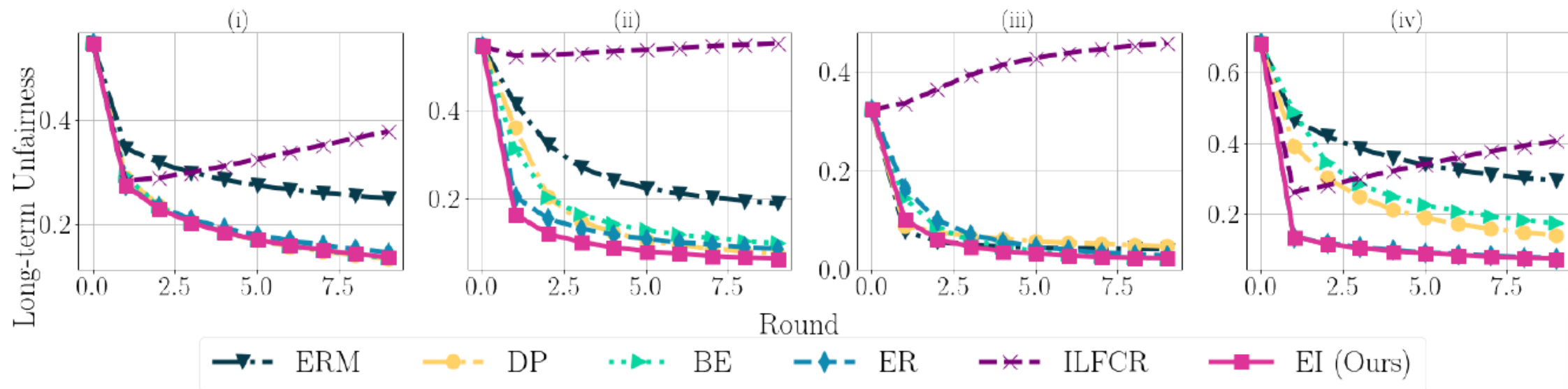
# Reproducibility experiments

- Reported (left side) and Reproduced (right side) Error rate and EI Disparity values of ERM and three proposed methods for achieving EI with a Logistic Regression model.

| Dataset       | Metric     | ERM  |      | Covariance-Based |      | KDE-Based   |             | Loss-Based |      |
|---------------|------------|------|------|------------------|------|-------------|-------------|------------|------|
| Synthetic     | Error Rate | .221 | .222 | .253             | .253 | .250        | .253        | .246       | .246 |
|               | EI Disp.   | .117 | .118 | .003             | .003 | .003        | .003        | .002       | .002 |
| German Stat.  | Error Rate | .220 | .262 | .262             | .262 | .243        | .249        | .237       | .237 |
|               | EI Disp.   | .041 | .021 | .021             | .022 | <b>.035</b> | <b>.226</b> | .015       | .016 |
| ACSIIncome-CA | Error Rate | .184 | .185 | .200             | .200 | .196        | .196        | .193       | .195 |
|               | EI Disp.   | .031 | .031 | .008             | .008 | .005        | .005        | .006       | .006 |

# Reproducibility Experiments

- The disparity between the sensitive group feature distributions reduces faster for the EI classifier than for the other metrics.
- This indicates that EI classifier is more favorable for achieving long-term fairness.



# Reproducibility Experiments

- Error rate and EI disparities of ERM and the proposed EI-regularized methods on an overparameterized Multilayer perceptron (MLP) using a subset of German Statlog Credit dataset.

| Metric         | ERM             | Covariance-Based | KDE-Based       | Loss-Based      |
|----------------|-----------------|------------------|-----------------|-----------------|
| Train Error    | .218 $\pm$ .004 | .233 $\pm$ .003  | .226 $\pm$ .009 | .233 $\pm$ .012 |
| Test Error     | .218 $\pm$ .010 | .218 $\pm$ .010  | .222 $\pm$ .007 | .231 $\pm$ .007 |
| Train EI Disp. | .024 $\pm$ .017 | .018 $\pm$ .011  | .018 $\pm$ .012 | .009 $\pm$ .009 |
| Test EI Disp.  | .064 $\pm$ .036 | .050 $\pm$ .024  | .070 $\pm$ .050 | .062 $\pm$ .015 |

# Reproducibility experiments

1



El Disparity and Loss  
value check

(Claim 1)

2



Long-term  
(un)fairness check

(Claim 2)

3



Overfitting  
robustness check

(Claim 3)

# Extended analysis

1

Evaluating EI  
Disparity and Error  
Rate values on a  
different dataset

(Claim 1)

2

Adding another  
sensitive feature

(Claim 1)

3

Long-term fairness  
with multiple  
sensitive features

(Claim 2)

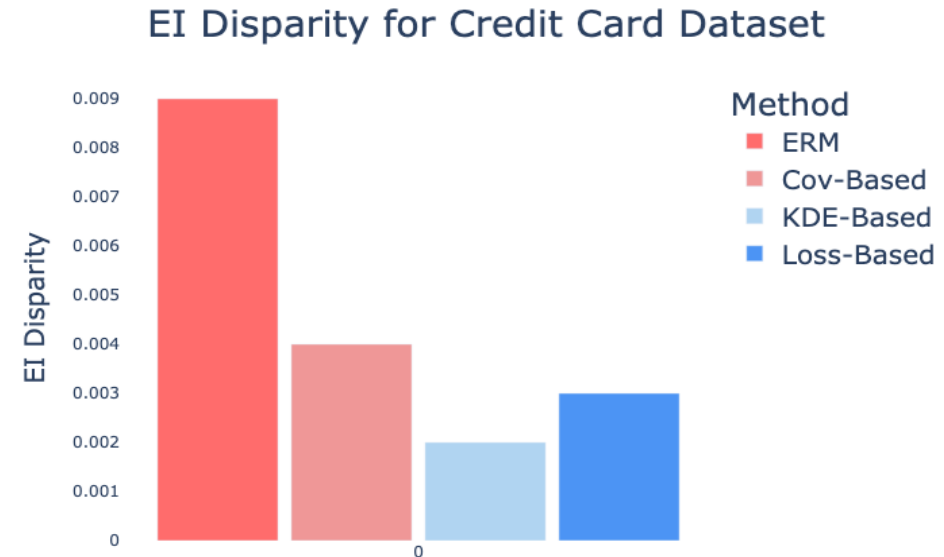
4

Overfitting  
robustness check  
with a more  
complex model

(Claim 3)

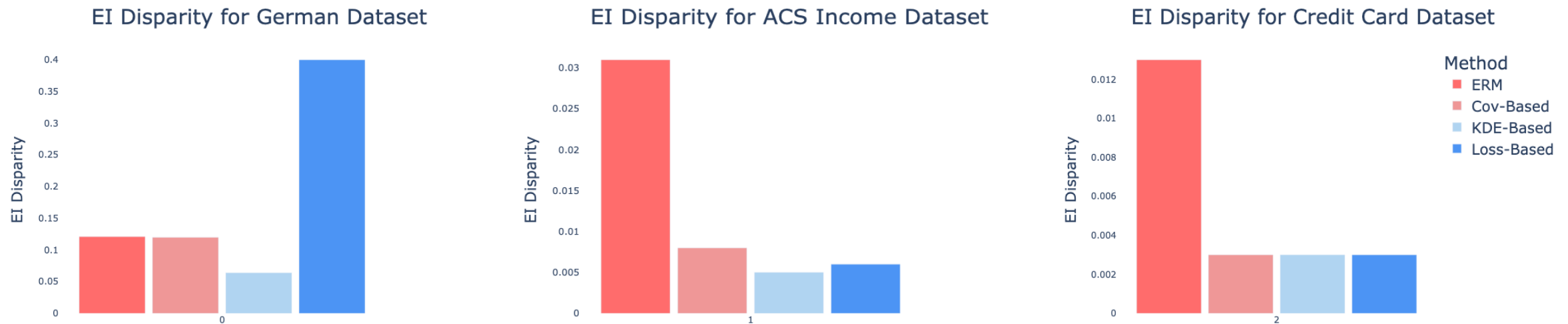
# Result 1 – EI Disparity and Error Rate values on a different datasets

- EI-based classifiers still have a lower EI disparity without causing a significant increase in the error rate on the new dataset.



# Result 2 – Adding another sensitive feature (Sex and Age)

- The measured EI Disparity for the original datasets using ERM and each of the 3 penalty terms optimized for 2 sensitive features.





## Result 2 – Adding another sensitive feature (Sex and Age)

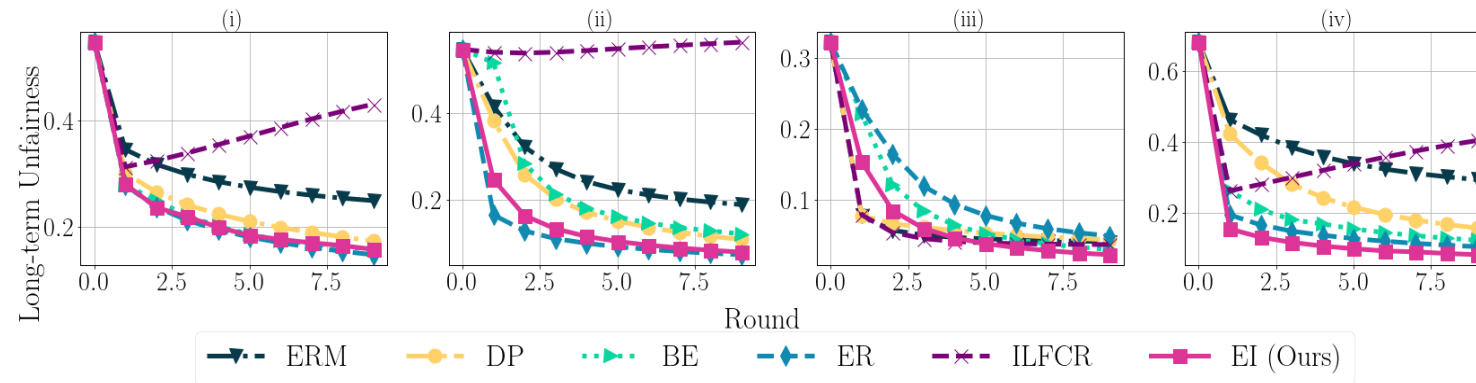
- The results indicate that EI Disparity of the proposed methods can still be low, without significantly increasing the Error Rate even with 2 sensitive features.



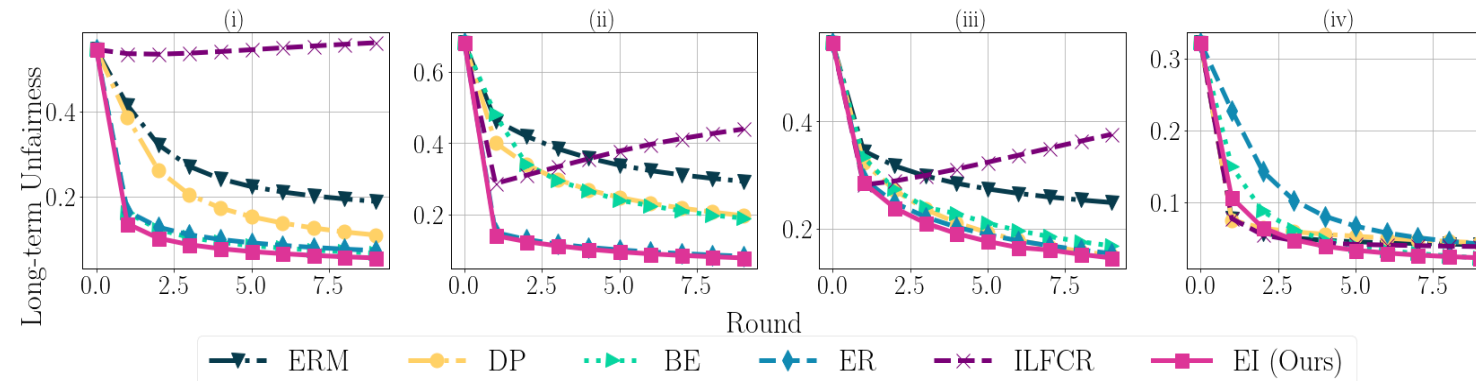
# Result 3 – Long Term fairness with multiple sensitive features

The disparity between the feature distributions of different sensitive groups reduces faster for the EI classifier

Feature 1



Feature 2



## Result 4 – Overfitting robustness

- Error rate and EI disparities of ERM and the proposed EI-regularized methods on an overparameterized Multilayer perceptron (MLP) using a subset of ACS-Income dataset.
- The error rate and EI disparity values for all methods are indicative of overfitting



# Conclusion

- The reproducibility study proved the general claims of the original paper.
- Experiments on a different dataset also support the claims.
- Experiments with 2 sensitive features produced the results that were in line with the authors' claims except for the Loss-based method.
- Further experiments did not substantiate EI's robustness to overfitting.



**Thank you for your attention!**