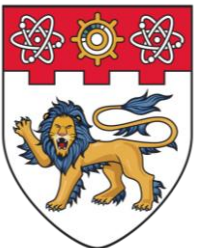


# Membership Inference on Text-to-Image Diffusion Models via Conditional Likelihood Discrepancy

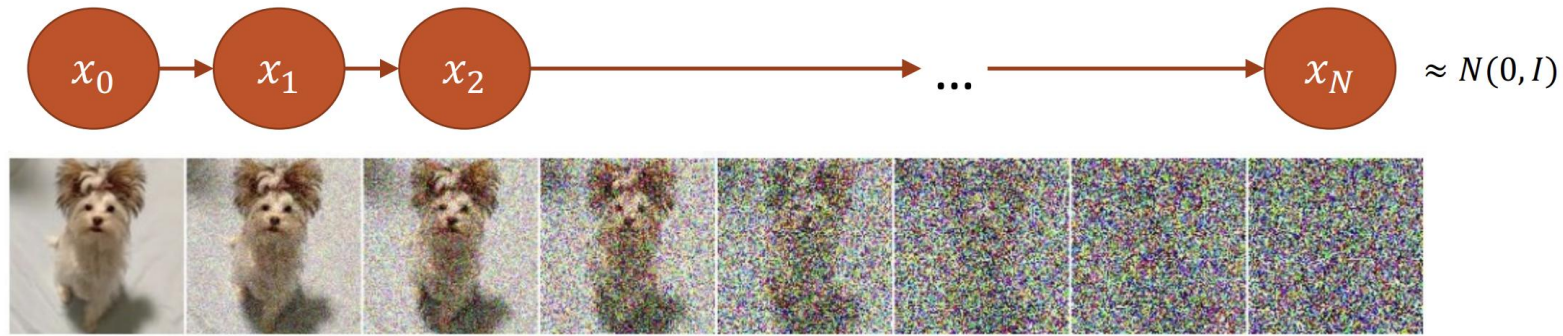
Shengfang Zhai, Huanran Chen, Yinpeng Dong✉, Jiajun Li,  
Qingni Shen✉, Yansong Gao, Hang Su, Yang Liu



# Content

- Motivation: Why we need ***Membership Inference (MI)*** for T2I models?
- + Background
- Key intuition: Conditional Overfitting
- Methods
- Experiments
- Conclusion

# Diffusion models



## ➤ Training objective is simple (MSE loss, Evidence Lower Bound)

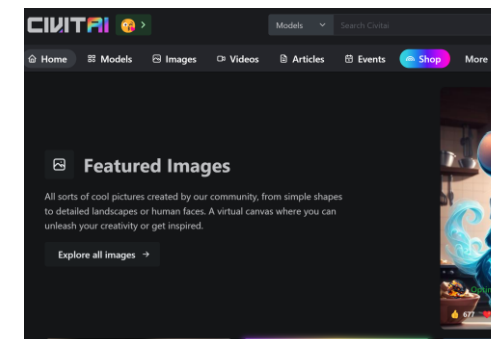
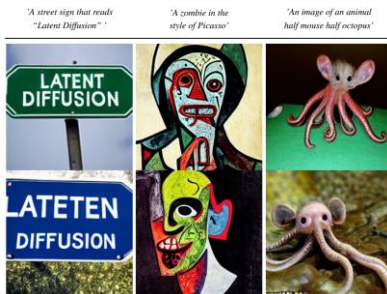
Unconditional Diffusion Models  
(DDPM):

$$\log p_{\theta}(\mathbf{x}_0) \geq \mathbb{E}_{q(\mathbf{x}_{1:T}|\mathbf{x}_0)} \left[ \log \frac{p_{\theta}(\mathbf{x}_{0:T})}{q(\mathbf{x}_{1:T} | \mathbf{x}_0)} \right] = -\mathbb{E}_{\epsilon, t} [||\epsilon_{\theta}(\mathbf{x}_t, t) - \epsilon||^2] + C,$$

Conditional Diffusion Models  
(T2I Models):

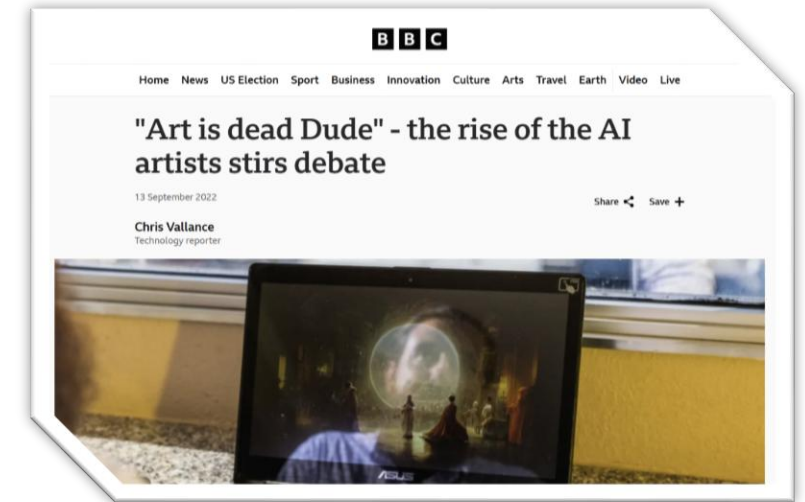
$$\log p_{\theta}(\mathbf{x}_0|\mathbf{c}) \geq -\mathbb{E}_{\epsilon, t} [||\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}) - \epsilon||^2] + C.$$

Simple but effective.



# Why we need *Membership Inference* on Text-to-image diffusion models?

- Unauthorized data usage auditing:  
Issues about copyright infringement [1,2,3...]
- Exploring memorization in T2I models:



[1] BBC. "Art is dead Dude" - the rise of the AI artists stirs debate. 2022. URL <https://www.bbc.com/news/technology-62788725>.

[2] CNN. AI won an art contest, and artists are furious. 2022. URL <https://www.cnn.com/2022/09/03/tech/ai-art-fair-winner-controversy/index.html>.

[3] Reuters. Lawsuits accuse AI content creators of misusing copyrighted work. 2023. URL <https://www.reuters.com/legal/transactional/lawsuits-accuse-ai-content-creators-misusing-copyrighted-work-2023-01-17/>.

[4] WashingtonPost. He made a children's book using AI. Then came the rage. 2022. URL <https://www.washingtonpost.com/technology/2023/01/19/ai-childrens-book-controversy-chatgpt-midjourney/>.

# Membership Inference:

*Is this **data point** used to train the **target model**?*

In **traditional tasks**:

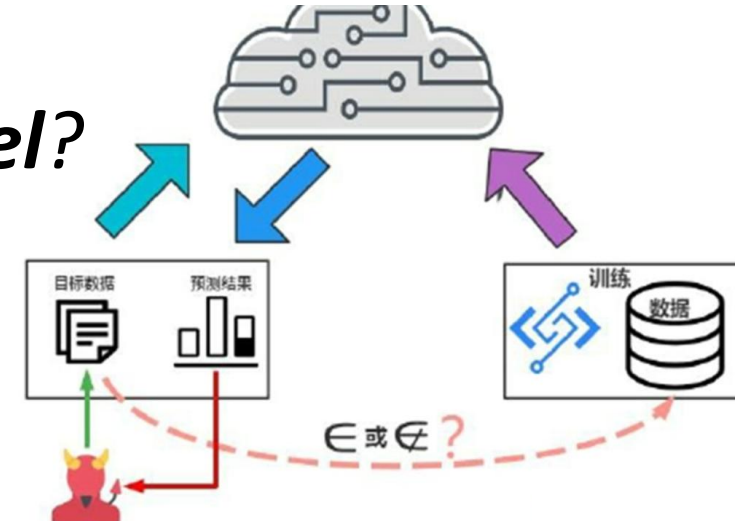
For a given data point  $\mathbf{x}$ :

$$\mathcal{M}(\mathbf{x}, f_{\theta}) = \mathbb{1} [\mathcal{M}'(\mathbf{x}, f_{\theta}) > \tau]$$

In **text-to-image synthesis**:

For a given data pair (image, text)  $\rightarrow (\mathbf{x}, \mathbf{c})$

$$\mathcal{M}(\mathbf{x}, \mathbf{c}, f_{\theta}) = \mathbb{1} [\mathcal{M}'(\mathbf{x}, \mathbf{c}, f_{\theta}) > \tau]$$



# Are existing works good enough?

- Only targeting at small-scale diffusion model <sup>[1]</sup> (NOT text-to-image)
- Unrealistic evaluation setting → **Hallucination of success!**
  1. Over-training
  2. Distribution shift

| Methods              | Evaluation (Fine-tuning)             | Evaluation (Pretraining)                                           |
|----------------------|--------------------------------------|--------------------------------------------------------------------|
| SecMI <sup>[2]</sup> | ~ 60 Epochs ( <b>Over-training</b> ) | LAION / COCO as mem/hold-out set ( <b>Different distribution</b> ) |
| PIA <sup>[3]</sup>   | N/A                                  | LAION / COCO as mem/hold-out set ( <b>Different distribution</b> ) |
| PFAMI <sup>[4]</sup> | ~ 60 Epochs ( <b>Over-training</b> ) | LAION / COCO as mem/hold-out set ( <b>Different distribution</b> ) |

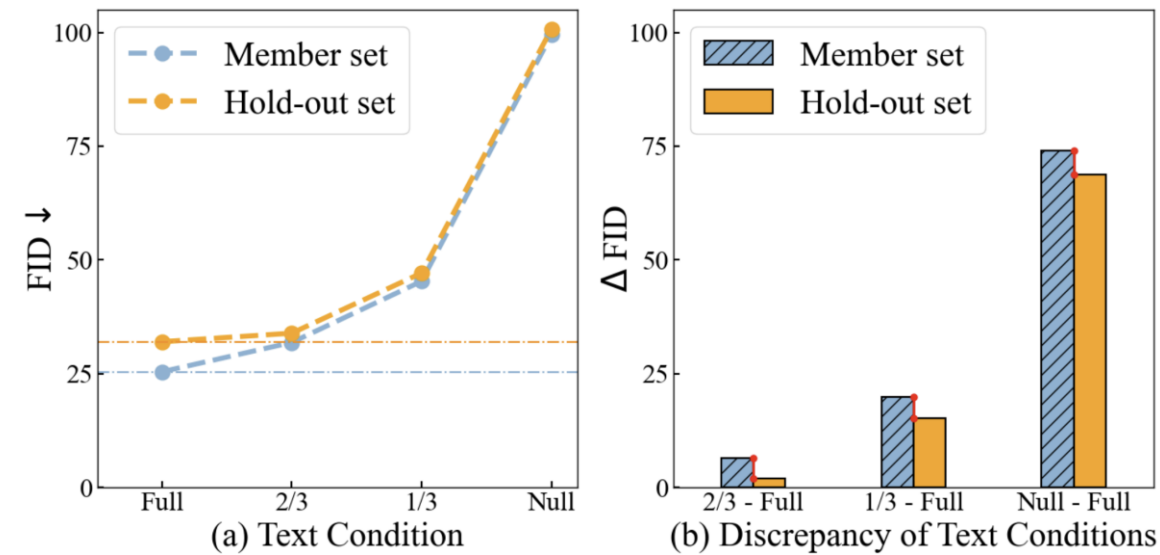
[1] Nicolas Carlini et al. Extracting training data from diffusion models. In 32nd USENIX Security Symposium (USENIX Security 23)

[2] Jinhao Duan et al. Are diffusion models vulnerable to membership inference attacks? In International Conference on Machine Learning, 2023.

[3] Fei Kong et al. An efficient membership inference attack for the diffusion model by proximal initialization. In The Twelfth International Conference on Learning Representations, 2024.

[4] Wenjie Fu et al. A probabilistic fluctuation based membership inference attack for generative models. arXiv preprint arXiv:2308.12143, 2023

# Conditional Overfitting



➤ Observation: T2I training process involves **Conditional Overfitting**.

**Training overfitting:**

$$D(q_{\text{mem}}(\mathbf{x}), p(\mathbf{x})) \leq D(q_{\text{out}}(\mathbf{x}), p(\mathbf{x}))$$

**Conditional overfitting:**

$$\underbrace{\mathbb{E}_{\mathbf{c}} [D(q_{\text{out}}(\mathbf{x}|\mathbf{c}), p(\mathbf{x}|\mathbf{c})) - D(q_{\text{mem}}(\mathbf{x}|\mathbf{c}), p(\mathbf{x}|\mathbf{c}))]}_{\text{overfitting to conditional distribution}} \geq \underbrace{D(q_{\text{out}}(\mathbf{x}), p(\mathbf{x})) - D(q_{\text{mem}}(\mathbf{x}), p(\mathbf{x}))}_{\text{overfitting to marginal distribution}}$$

*FID (Fréchet Inception Distance)*



# CLiD (Conditional Likelihood Discrepancy)

Using Kullback-Leibler (KL) divergence as the distance metric, we can get (Proof in Appendix B):

$$\mathbb{E}_{q_{mem}(\mathbf{x}, \mathbf{c})} [\log p(\mathbf{x}|\mathbf{c}) - \log p(\mathbf{x})] \geq \mathbb{E}_{q_{out}(\mathbf{x}, \mathbf{c})} [\log p(\mathbf{x}|\mathbf{c}) - \log p(\mathbf{x})] + \delta_H$$

Ignoring  $\delta_H$ , we have the indicator **CLiD**:

$$\mathbb{I}(\mathbf{x}, \mathbf{c}) = \log p(\mathbf{x}|\mathbf{c}) - \log p(\mathbf{x})$$

Using ELBOs to approximate likelihood:

$$\mathbb{I}(\mathbf{x}, \mathbf{c}) = \mathbb{E}_{t, \epsilon} [\|\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}_{null}) - \epsilon\|^2] - \mathbb{E}_{t, \epsilon} [\|\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}) - \epsilon\|^2]$$

To simplify computation, we directly estimate likelihood difference by Monte Carlo Sampling [1]:

$$\mathbb{I}(\mathbf{x}, \mathbf{c}) = \mathbb{E}_{t, \epsilon} [\|\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}_{null}) - \epsilon\|^2 - \|\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}) - \epsilon\|^2]$$



# CLiD-MI

$$\mathcal{D}_{\mathbf{x}, \mathbf{c}, \mathbf{c}_i^*} = \mathbb{E}_{t, \epsilon} [||\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}_i^*) - \epsilon||^2 - ||\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}) - \epsilon||^2], \quad \mathbb{C} = \{\mathbf{c}_1^*, \mathbf{c}_2^*, \dots, \mathbf{c}_k^*\}$$

$$\mathcal{L}_{\mathbf{x}, \mathbf{c}} = -\mathbb{E}_{t, \epsilon} [||\epsilon_{\theta}(\mathbf{x}_t, t, \mathbf{c}) - \epsilon||^2]$$

- Threshold-based CLiD<sub>th</sub>:

$$\mathcal{M}_{\text{CLiD}_{th}}(\mathbf{x}, \mathbf{c}) = \mathbb{1} \left[ \alpha \cdot \mathcal{S}\left(\frac{1}{k} \sum_i^k \mathcal{D}_{\mathbf{x}, \mathbf{c}, \mathbf{c}_i^*}\right) + (1 - \alpha) \cdot \mathcal{S}(\mathcal{L}_{\mathbf{x}, \mathbf{c}}) > \tau \right]$$

- Vector-based CLiD<sub>vec</sub>:

$$\mathbf{V} = (\mathcal{D}_{\mathbf{x}, \mathbf{c}, \mathbf{c}_1^*}, \mathcal{D}_{\mathbf{x}, \mathbf{c}, \mathbf{c}_2^*} \dots \mathcal{D}_{\mathbf{x}, \mathbf{c}, \mathbf{c}_k^*}, \mathcal{L}_{\mathbf{x}, \mathbf{c}})$$

$$\mathcal{M}_{\text{CLiD}_{vec}}(\mathbf{x}, \mathbf{c}) = \mathbb{1} \left[ \mathcal{J}_{\mathcal{M}}(\mathbf{V}) > \tau \right]$$

# Main Experiments

## ➤ Settings

1. Fine-tuning (Over-training): consistent with exiting works  
Data (member/hold-out set Size): Pokemon (~400), COCO (2500), Flickr (2500);  
Training steps: 15,000, 150,000, 150,000  
No augmentation.
2. Fine-tuning (Real-world training): following Huggingface scripts <sup>[1]</sup>  
Data (member/hold-out set Size): Pokemon (~400), COCO (2500), Flickr (100,000);  
Training steps: 7,500, 50,000, 200,000  
Default augmentation.
3. Pretraining (Ensuring the distribution consistency).

## ➤ Metrics

ASR, AUC, TPR@1%FPR

[1] Huggingface. The training script of stable-diffusion, 2024. URL <https://huggingface.co/docs/diffusers/training/text2image#launch-the-script>. Accessed: May 22, 2024.

Table 1: Results under *Over-training* setting. We mark the best and second-best results for each metric in **bold** and underline, respectively. Additionally, the best results from baselines are marked in blue for comparison.

| Method              | MS-COCO      |              |              | Flickr             |              |              | Pokemon      |              |              | Query |
|---------------------|--------------|--------------|--------------|--------------------|--------------|--------------|--------------|--------------|--------------|-------|
|                     | ASR          | AUC          | TPR@1%FPR    | ASR                | AUC          | TPR@1%FPR    | ASR          | AUC          | TPR@1%FPR    |       |
| Loss                | 81.92        | 89.98        | 32.28        | 81.90              | 90.34        | 40.80        | 83.76        | 91.79        | 25.77        | 1     |
| PIA                 | 68.56        | 75.12        | 5.08         | 68.56              | 75.12        | 5.08         | 83.37        | 90.95        | 13.31        | 2     |
| M. C.               | 82.04        | 89.77        | 36.04        | 83.32              | 91.37        | 41.20        | 79.35        | 86.78        | 23.74        | 3     |
| SecMI               | 83.00        | 90.81        | 50.64        | 62.96 <sup>†</sup> | 89.29        | 48.52        | 80.49        | 90.64        | 9.36         | 12    |
| PFAMI               | 94.48        | 98.60        | 78.00        | 90.64              | 96.78        | 50.96        | 89.86        | 95.70        | 65.35        | 20    |
| CLiD <sub>th</sub>  | 99.08        | <b>99.94</b> | <b>99.12</b> | 91.42              | 97.39        | <b>74.00</b> | <b>97.96</b> | 99.28        | <b>97.84</b> | 15    |
| CLiD <sub>vec</sub> | <b>99.74</b> | 99.31        | 95.20        | <b>91.78</b>       | <b>97.52</b> | 73.88        | 97.36        | <b>99.46</b> | 96.88        | 15    |

<sup>†</sup> When conducting SecMI [15], we observe that the thresholds obtained on the shadow model sometimes do not transfer well to the target model.

## Over-training:

1. No obvious effectiveness difference of MI methods (Query 1 vs Query 12)
2. Excessive and unrealistic overfitting.

***Fail to adequately reflect the effectiveness differences among various methods !***

Table 2: Results under *Real-world training* setting. We also highlight key results according to Tab. 1.

| Method              | MS-COCO |       |           | Flickr |       |           | Pokemon |       |           | Query |
|---------------------|---------|-------|-----------|--------|-------|-----------|---------|-------|-----------|-------|
|                     | ASR     | AUC   | TPR@1%FPR | ASR    | AUC   | TPR@1%FPR | ASR     | AUC   | TPR@1%FPR |       |
| Loss                | 56.28   | 61.89 | 1.92      | 54.91  | 56.60 | 1.83      | 61.03   | 65.96 | 2.82      | 1     |
| PIA                 | 54.10   | 55.52 | 1.76      | 51.96  | 52.73 | 1.28      | 58.34   | 59.95 | 2.64      | 2     |
| M. C.               | 57.98   | 61.97 | 2.64      | 54.92  | 56.78 | 2.16      | 61.10   | 66.48 | 3.84      | 3     |
| SecMI               | 60.94   | 65.40 | 3.92      | 55.60  | 63.85 | 2.76      | 61.28   | 65.56 | 0.84      | 12    |
| PFAMI               | 57.36   | 60.39 | 2.72      | 54.68  | 56.13 | 1.80      | 58.94   | 63.53 | 5.76      | 20    |
| CLiD <sub>th</sub>  | 88.88   | 96.13 | 67.52     | 87.12  | 94.74 | 53.56     | 86.79   | 93.28 | 61.39     | 15    |
| CLiD <sub>vec</sub> | 89.52   | 96.30 | 66.36     | 88.86  | 95.33 | 53.92     | 85.47   | 92.61 | 59.95     | 15    |

| Method             | LAION |       |           | Query |
|--------------------|-------|-------|-----------|-------|
|                    | ASR   | AUC   | TPR@1%FPR |       |
| Loss               | 51.78 | 50.90 | 1.75      | 1     |
| PIA                | 52.13 | 52.42 | 1.25      | 2     |
| M. C.              | 53.18 | 53.96 | 1.25      | 3     |
| SecMI              | 57.43 | 58.59 | 2.45      | 12    |
| PFAMI              | 59.08 | 61.11 | 1.45      | 20    |
| CLiD <sub>th</sub> | 64.53 | 67.82 | 5.01      | 15    |

Table 3: The performance of membership inference methods on Stable Diffusion v1-5 [47] in pretraining setting. We utilize the processed LAION dataset to ensure the distribution consistency between member / hold-out sets [13, 16]. The best results are highlighted in **bold**.

Real-world training & Pretraining setting:  
*Outperforming the baselines across all three metrics*

# Other Experiments

## 1. Effectiveness trajectory

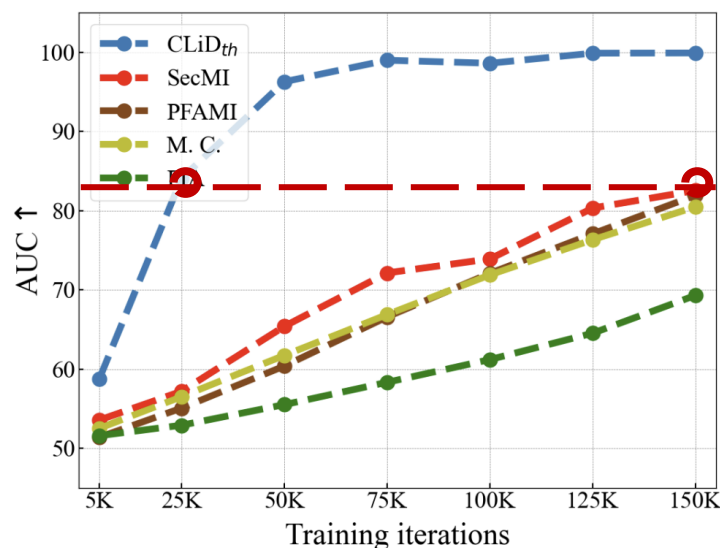


Figure 2: Effectiveness trajectory on various training steps.

## 2. Ablation Study

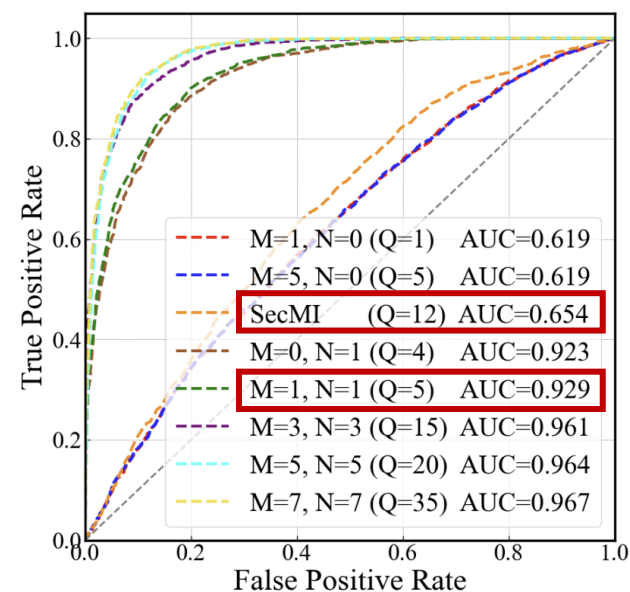


Figure 3: Performance of CLiD<sub>th</sub> and SecMI under various Monte Carlo sampling numbers (i.e., query count). The legend labels are sorted in ascending order by AUC values.

# Other Experiments

## 3. Resistance to Defense

Table 4: The performance of different methods under no augmentation and default augmentation.

| Method             | No Augmentation |       |           | Default Augmentation   |                        |                             |
|--------------------|-----------------|-------|-----------|------------------------|------------------------|-----------------------------|
|                    | ASR             | AUC   | TPR@1%FPR | ASR ( $\Delta$ )       | AUC ( $\Delta$ )       | TPR@1%FPR ( $\Delta$ )      |
| Loss               | 66.54           | 72.73 | 7.72      | 56.28 (-10.26)         | 61.89 (-10.84)         | 1.92 (-5.80)                |
| PIA <sup>†</sup>   | 56.56           | 59.28 | 2.00      | 54.10 (-2.46)          | 55.52 (-3.76)          | 1.76 (-0.24)                |
| SecMI              | 72.02           | 81.07 | 13.72     | 60.94 (-11.08)         | 65.40 (-15.08)         | 3.92 (-9.80)                |
| PFAMI              | 79.20           | 87.05 | 18.44     | 57.36 (-21.84)         | 60.39 (-26.66)         | 2.72 (-15.72)               |
| CLiD <sub>th</sub> | 96.76           | 99.47 | 91.72     | 88.88 ( <b>-7.88</b> ) | 96.13 ( <b>-3.34</b> ) | 67.52 (-24.20) <sup>‡</sup> |

<sup>†</sup>We omit the discussion of PIA as it shows no effectiveness at this training steps, with the metrics consistently approximating random guessing.

<sup>‡</sup>The TPR@1%FPR value changes significantly here because its ROC curve is very sharp when FPR close to 0.

*Stronger resistance to data augmentation*

Table 5: Effectiveness of CLiD<sub>th</sub> in adaptive defense. We calculate the FID [20] with 10,000 unseen MS-COCO samples to assess the model utility.

| Defense | CLiD <sub>th</sub> on MS-COCO |       |           | FID ↓ / $\Delta$                  |
|---------|-------------------------------|-------|-----------|-----------------------------------|
|         | ASR                           | AUC   | TPR@1%FPR |                                   |
| None    | 88.88                         | 96.13 | 67.52     | 13.17                             |
| Reph    | 85.32                         | 93.83 | 55.67     | 13.58 / <b>+0.41</b>              |
| Del-1   | 86.40                         | 93.59 | 59.52     | 13.18 / <b>-0.01</b>              |
| Del-3   | 83.91                         | 91.52 | 52.03     | 12.92 / <b>-0.25</b>              |
| Shuffle | 65.89                         | 67.37 | 0.15      | 18.26 / <b>+5.09</b> <sup>†</sup> |

<sup>†</sup>Compared to other methods, the increase in FID caused by shuffling is unacceptable for generative models.

*Resistance to adaptive defense*

# Other Experiments

## 4. Weaker Assumption:

What if we don't have groundtruth text?

→ Use Image-Caption model (BLIP) to generate Pseudo-Text.

| Images                                                                              | Text                                                                                                                                                                                                                                                                                           |
|-------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  | <p>Groundtruth Text (MS-COCO): <i>A big burly grizzly bear is show with grass in the background.</i></p> <p>Generated by BLIP: <i>A brown bear sitting on the grass.</i></p> <p>Generated by GPT4o-mini: <i>A close-up of a large brown bear with thick fur, sitting in a grassy area.</i></p> |
|  | <p>Groundtruth Text (MS-COCO): <i>A large white bowl of many green apples.</i></p> <p>Generated by BLIP: <i>A bowl of green apples.</i></p> <p>Generated by GPT4o-mini: <i>A bowl filled with fresh, shiny green apples stacked on top of each other.</i></p>                                  |
|  | <p>Groundtruth Text (MS-COCO): <i>A little girl holds up a big blue umbrella.</i></p> <p>Generated by BLIP: <i>A young girl holding an umbrella.</i></p> <p>Generated by GPT4o-mini: <i>A young girl holds a blue umbrella while wearing a pink jacket and jeans.</i></p>                      |

Table 6: Results without access to the corresponding text under *Over-training* setting and *Real-world training* setting. We fine-tune MS-COCO on SDv1-4. Key results are highlighted as Tab. 1.

| Method              | <i>Over-training</i> (Pseudo-Text) |       |           | <i>Real-world training</i> (Pseudo-Text) |       |           | Query |
|---------------------|------------------------------------|-------|-----------|------------------------------------------|-------|-----------|-------|
|                     | ASR                                | AUC   | TPR@1%FPR | ASR                                      | AUC   | TPR@1%FPR |       |
| Loss                | 73.80                              | 81.01 | 9.71      | 56.08                                    | 58.47 | 1.60      | 1     |
| PIA                 | 61.40                              | 65.75 | 1.20      | 53.44                                    | 54.38 | 1.52      | 2     |
| M. C.               | 74.36                              | 81.55 | 11.28     | 56.68                                    | 60.00 | 1.28      | 3     |
| SecMI               | 82.04                              | 88.97 | 40.80     | 60.48                                    | 64.04 | 3.28      | 12    |
| PFAMI               | 91.56                              | 95.16 | 68.16     | 58.12                                    | 59.77 | 2.64      | 20    |
| CLiD <sub>th</sub>  | 92.84                              | 95.43 | 72.36     | 76.16                                    | 83.27 | 19.76     | 15    |
| CLiD <sub>vec</sub> | 93.26                              | 96.59 | 71.73     | 77.76                                    | 84.48 | 18.06     | 15    |



# Conclusion

1. Identifying ***Conditional Overfitting***, i.e., T2I diffusion models overfit more to conditional distribution  $p(x, y)$  than to marginal distribution  $p(x)$
2. Revealing the ***hallucination success*** of existing membership inference methods and providing a more reasonable evaluation setting
3. Proposing to conduct membership inference via Conditional Likelihood Discrepancy (CLiD). CLiD-MI significantly **outperforms baselines across various data distributions and scales**.

# Limitation

Superiority of CLiD-MI over the baselines in the pretraining setting ***is not as evident*** compared to fine-tuning setting.

→ We emphasize our experiments under pretraining setting (Tab. 3) reveal the hallucination success of existing works and ***encourage future research to focus on this more challenging and practical scenario***.

# Thanks!

*Paper*



*Repository*



shengfang.zhai@gmail.com